Polynomials and Collecting Like Terms

		ent and <u>variable</u> par	rt		
Type equa <i>EX/ 3x</i>	$5x^2$	11	-lx	5 <i>a</i> l	b
A polynomial is a	collection of on	e or more terms join	ed by addition or	subtraction	
<i>EX</i> / 5x ²	2x + (-1)	$3x^2 + (-2x) + 1$	a + (-	-2b) + c	$54x^{3}y^{2} + (-3x^{4}y^{1})$
BEWARE THE IN $x \rightarrow 1x$	_	(x + 4)	$\rightarrow 1(x+4)$	-(x-3)	$\rightarrow -1(x-3)$
		YLES THAT MEAN $\leftrightarrow \rightarrow +(-x)$			
Like terms have i	dentical variable	parts. <u>Unlike term</u> s	s have different va	riable parts.	
EX/ Which of the	following are "li	ke terms"?			
5x 7xy	-3x 3.2	11x ² x	$-4x^{2}$	3x ³ -3	3xy x ²
Collecting like teri Only add/subtract				he like term	<i>s</i> .
PART 1/ Collect th a) $2x + 3x$	ne like terms an	d write in the simp	•	- (-1) + (-	-2 <i>c</i>) + 4
b) $4x + (-1x)$.)		h) $4t^2$	+2+(-2t)	$) + t^2 + 3t - 1$
c) $2x + 1 + 6$	(-3) + (-3x)		i) 3d +	(-2) + (-10	d) + (-2d)
d) $2x^2 + x^2$	$-4x^{2}$		j) 3 – 2	$2\mathbf{c} + 2\mathbf{c}^2 - \mathbf{c}^2$	+ c + 1
e) $-x^2 + 2x$	$x-2x^2-4x$		k) 2x +	2 + 2x + 3 - 3	- 4x - 2
f) $4c - 2c - 3c - 3c - 3c - 3c - 3c - 3c - 3$	+ 3 + <i>c</i>		l) —3и	$v + 1 + 2w^2$	$^{2} + 5w - 3$

m)
$$-3r - 2r + r^2 + r - 3r^2$$

n) $(-3y) + (-y^2) - 4 + y + 3y^2$

PART 2/ Collect the like terms. a) 7m + 5m

e)
$$x + y + (-z) + y + (-xy) + (-x) + (-z)$$

b)
$$3u + 2v + (-u) + (-6v)$$

f) $2x^2 - 5 - x^2 - 1x^2 + 4x + 4$

c)
$$-x - 8y + 6x + 11 - 4y$$

g) $(-3xy) + (-2xy) + xy$

d)
$$2x^3 + 3x^4 + 5x^3 - 5x^4$$

h) $2x^2y + 3xy^2 - 1xy^2 - 4x^2y$

i)
$$-3r^2 + (-4pr) + 4p^2 + (-7pr) + r^2 + (-5p^2)$$

j)
$$-2r + 4x^2 + 3x - 1r^2 + (-3r) + (-x^2) + r - 4x$$

	41		
	$-xt^2 - tr^2 - tx - i$		i) $-2r^2 - tp^2 - i\eta$
$_{z}\Lambda x_{z} + \Lambda_{z}x_{z} - (q$	<i>Кх</i> ₇ - (З	f – x4 (f	e) $2\gamma - 2z - 1xy$
d) $7x^3 - 2x^2$	c) $5x - 12y + 11$	nz + ab - (d	m21 (b
			PART 2

			C T T A A
		4 – 42 – ² 42 (u	n4 – ² n2 – (m
		$1c^{2} + (2c) + c^{2}$	
$2 - w2 + ^{2}w2$ (1	қ) 3	i) $1c^2 - 1c + 4$ or	2- (i
			e) $-3x^2 - 2x$
$\mathbf{p} = \mathbf{r} + \mathbf{r} + \mathbf{r}$	g) 2c+3	f) 3c + 3	e) -3x ² - 2x
	or - 1x + (-2)		
q) -Jx ²	z - xt - (s)	<i>x</i> ɛ (q	xg (b
			Answers

wenA ŀ

Name:

<u>MPM1D – Distribi</u>	<u>itive Property</u>	<u>Name:</u>	
The distributive	e property states that:	Example: $3(x+4)$	
a(x +	y) = ax + ay	=3x+12	2
Expand each of the foll	owing. Your final answer should	have no brackets.	
1. $2(x+1)$	2. $2(x+3)$	3) 3(<i>x</i> -1)	4) $4(1+2x)$
5) $-2(x-2)$	6) $-2(x+2)$	7) $-3(x+1)$	8) $-1(x+5)$
,	, , ,		
9) 2(1+3 <i>x</i>)	10) $-3(x-1)$	11) -2(2x-1)	12) $-2(3-x)$
(12) = x(11 + 2)	(14) $r(2 + r)$	15) x(2x 1)	$(1, 1) \cdots (1, 2, 1)$
13) $x(x+3)$	14) $x(2+x)$	15) $x(3x-1)$	16) $x(4-2x)$
17) $2x(x+3)$	18) $2x(3-x)$	19) $-2x(x+1)$	20) $-3x(2x-1)$

PART A: Add the following polynomials.					
1. $(x+1) + (3x-1)$	3.	(4-2x) + (-x+1)			
2. $(2x-3) + (x-1)$	4.	$(2x^2 + 3x - 1) + (x^2 - x + 1)$			
PART B: Expand the following. A	fter expanding, the brac	kets should be gone.			
5. $-(x+3)$	7.	-(2x-3)			
6. $-(2-x)$	8.	$-(x^2+4-3x)$			
PART C: Expand the following.					
9. $3(x+1)$	1	1. $-2(x^2+x-3)$			
	_				
10. $-2(2x+1)$	12	2. $x(-2x+1)$			
	-				

PART D: Subtract the polynomials. Expand and collect, or "add the opposite"

13. (x+2) - (2x+1)15. $(2+x^2) - (3x^2+1)$

14. (3x-1)-(2x-1)16. $(2x^2-2x+3)-(-x^2-4x+1)$ 17. (-2x+4) - (6-2x)

19.
$$(5y+2) - (2y^2 + 3y - 1)$$

18.
$$(3x^2 + 2x) - (2x^2 - 2x + 1)$$

20. $(-5z^2 + 3z - 1) - (3z^2 - 3z - 8)$

PART E: Expand and collect like terms.

 21.
$$2(x+1) + 3(x-1)$$
 24. $3(x-2) - 2(2x+1)$

22.
$$-2(x+2) + (4x+3)$$
 25. $2x(x-4) + x(x+3)$

23.
$$-2(2x+1)+3(-1+2x)$$
 26. $-3z(z-2)-(z^2-2z+5)$

ANSWERS ANSWERS ANSWERS!!!

1. 4 <i>x</i>	2. $3x - 4$	3. $-3x + 5$	4. $3x^2 + 2x$	5. $-x-3$	6. $x - 2$	7. $-2x+3$
8. $-x^2 - 4 + 3x$	9. $3x + 3$	10. $-4x-2$	11. $-2x^2 - 2x + 6$	12. $-2x^2 + x$	13. $-x+1$	14. <i>x</i>
15. $-2x^2 + 1$	16. $3x^2 + 2x + 2$	17. –2	18. $x^2 + 4x - 1$	19. $-2y^2 + 2y + 3$	20. $-8z^2 + 6z^2$	z + 7
21. 5 <i>x</i> – 1	22. 2x-1	23. $2x-5$	24. $-x-8$	25. $3x^2 - 5x$	26. $-4z^2 +$	8z – 5

Name: _____

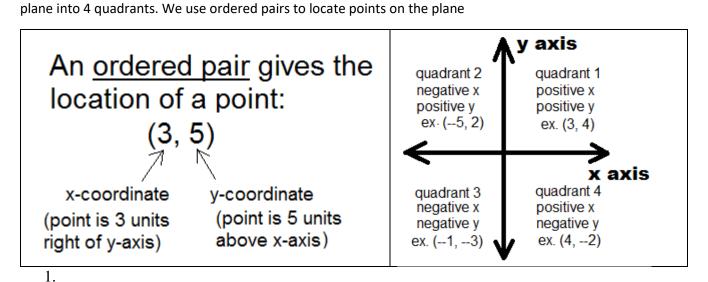
1.	2.
n+4-9-5n	
n + 4 - 9 - 5n	12r - 8 - 12
3. $-2x + 11 + 6x$	4. $12r + 5 + 3r - 5$
5.	4.
$\frac{1}{5}$ $\frac{4(1+9x)}{4(1+9x)}$	-6(x+4)
5. ((1 +)))	6. $-0(x + 4)$
7.	8.
-8(1-5x)	$(1-7n)\cdot 5$
9.	10.
x(-2x-3)	6v(2v+3)
11.	12.
(4+2n)+(5n+2)	$(9 + 5r^2 + 11r) + (9r - 2 - 8r^2)$
13.	14.
(5a+4) - (5a+3)	$(3a^2+1)-(4+2a^2)$
15.	16.
$(-7n^2 + 8n - 4) + (-11n + 2 - 14n^2)$	$(8k + k^2 - 6) - (-10k + 7 - 2k^2)$
17.	18.
$ \begin{array}{c} 17. \\ 3(x-4) + 2(5+x) \\ 19. \\ \end{array} $	3(x-2) + 5
19.	20.
1 + 2(x + 2)	3(y+1) + 6(2-y)
21.	22.
2(y-3) - 4(2y+1)	x(x+4) + 2(x-3)
23.	24.
2(b-a) + 3(a+b)	$-x^2 - x(x-2)$
25.	26.
2a - (a - 2b)	4x(x-3) - 2x(5-x)

Simplify each of the following. Use a different sheet of paper to show any steps.

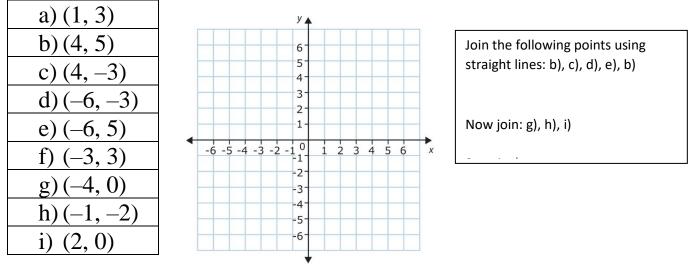
ANSWERS

1. $-4n - 5$	2. $12r - 20$	3. $4x + 11$	4. 15 <i>r</i>
5. $36x + 4$	6. $-6x - 24$	7. $40x - 8$	8. $-35n + 5$
9. $-2x^2$ –	10. $12v^2 + 18v$	11. 7 <i>n</i> + 6	$123r^2 + 20r + 7$
3 <i>x</i>			
13. 1	14. $a^2 - 3$	$1521n^2 - 3n - 2$	16. $3k^2 + 18k - 13$
17. 5 <i>x</i> − 2	18 . 3 <i>x</i> − 1	19. $2x + 5$	20. $-3y + 15$
21 . −6 <i>y</i> − 10	22. $x^2 + 6x - 6$	23. $a + 5b$	24. $-2x^2 + 2x$
25. <i>a</i> + 2 <i>b</i>	26. $6x^2 - 22x$		

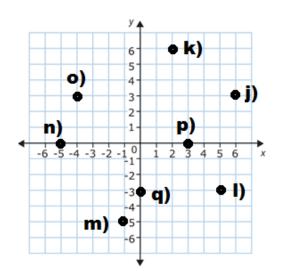
The imaginary lines we call the x-axis (which is horizontal) and y-axis (which is vertical), chop the Cartesian



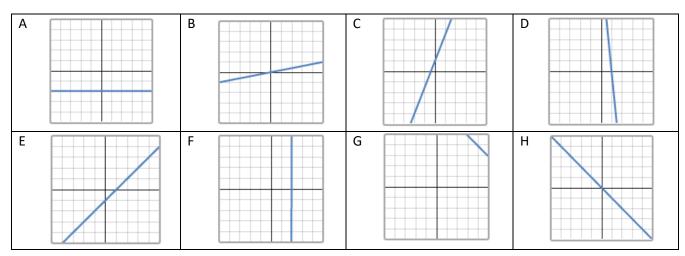
Mark the following points on the Cartesian plane.



2. State the coordinates of the points on the Cartesian plane.



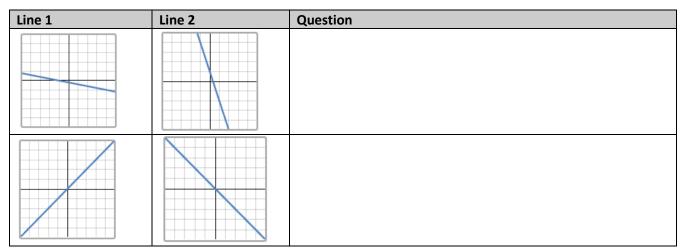
MPM1D – My Line Polygraph Name: ____



For each question and answer, identify the lines that could be eliminated. Use the lines above.

#	Question	Answer	Eliminated
1.	Is the line increasing?	Yes	
2.	Does the line pass through the origin?	No	
3.	Is the line steep?	No	
4.	Is the line decreasing?	Yes	
5.	Is the line either horizontal or vertical?	Yes	
6.	Is the line increasing and steep?	Yes	
7.	Does the line have a positive y-intercept?	No	
8.	Can you see the x- intercept in the picture?	Yes	

In each case, I will give you two lines that remain. Write a question that would let you win the game.



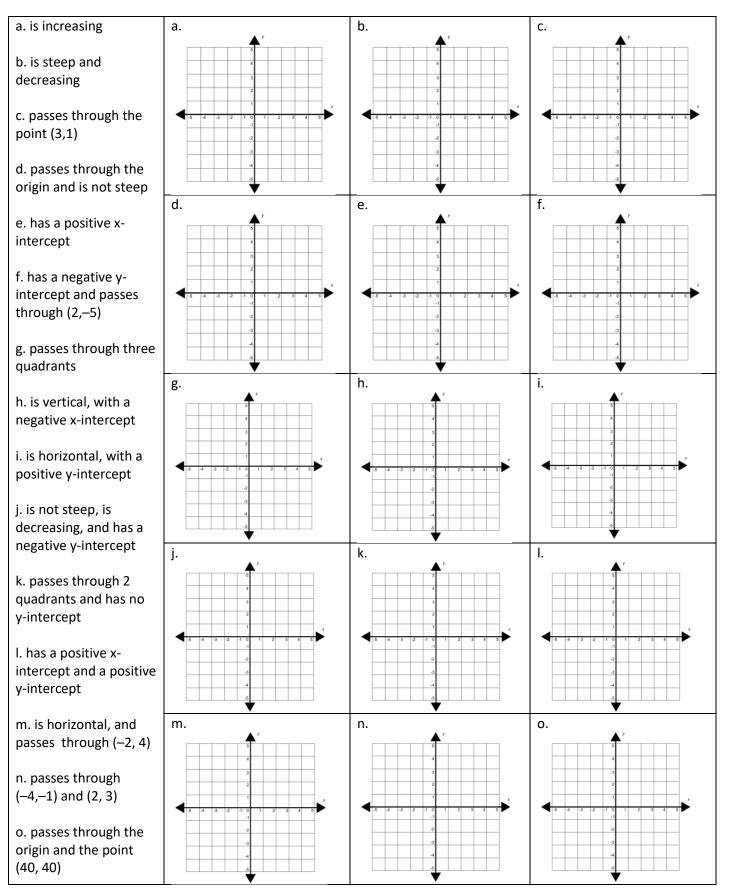
For each question, draw three lines (one for yes, two for no). Use a ruler.

Line 1 (Yes!)	Line 2 (No!)	Line 3 (No!)	Question
			Is the line steep and decreasing?
			Does the line have a positive x-intercept and a positive y-intercept?
			Does the line pass through 3 quadrants?

Steep	Not steep	Increasing	Decreasing
Vertical	Horizontal	x-intercept	y-intercept
Positive	Negative	Origin	Quadrant (1/2/3/4)
x-axis	y-axis		

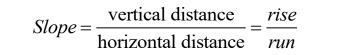
<u>MPM1D – Draw A Line That...</u>

Name: _____



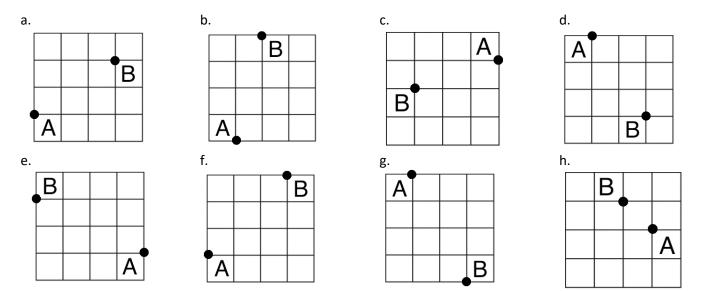
Slope - Introduction

In math, we have a way to determine/measure/represent the steepness of a line that connects two points. It is called "Slope", and it is can be found by finding the ratio of the vertical distance between two points to the horizontal distance between two points:

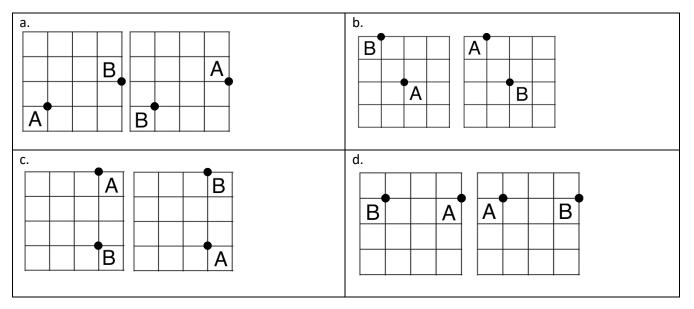


For the vertical distance ("rise")	For the horizontal distance ("run")
\rightarrow Moving upwards is positive	ightarrow Moving from left to right is positive
\rightarrow Moving downwards is negative	ightarrow Moving from right to left is negative

1. Find the slope between points A and B. Leave answers as <u>reduced</u> fractions ($\frac{1}{2}$ instead of $\frac{2}{4}$).



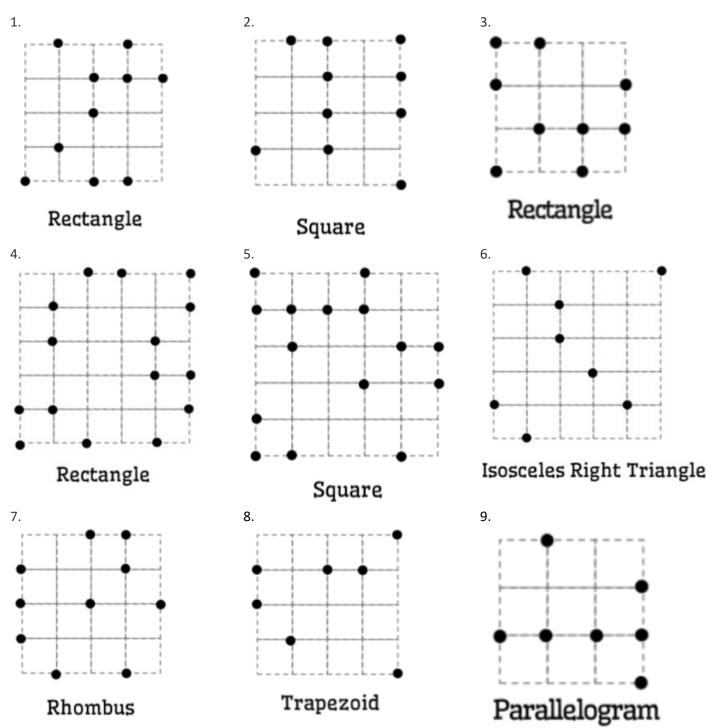
2. For each pair of graphs, find the slope from Point A to Point B. Compare your answers for each pair, then reflect. Remember to reduce your slopes to simplest form.

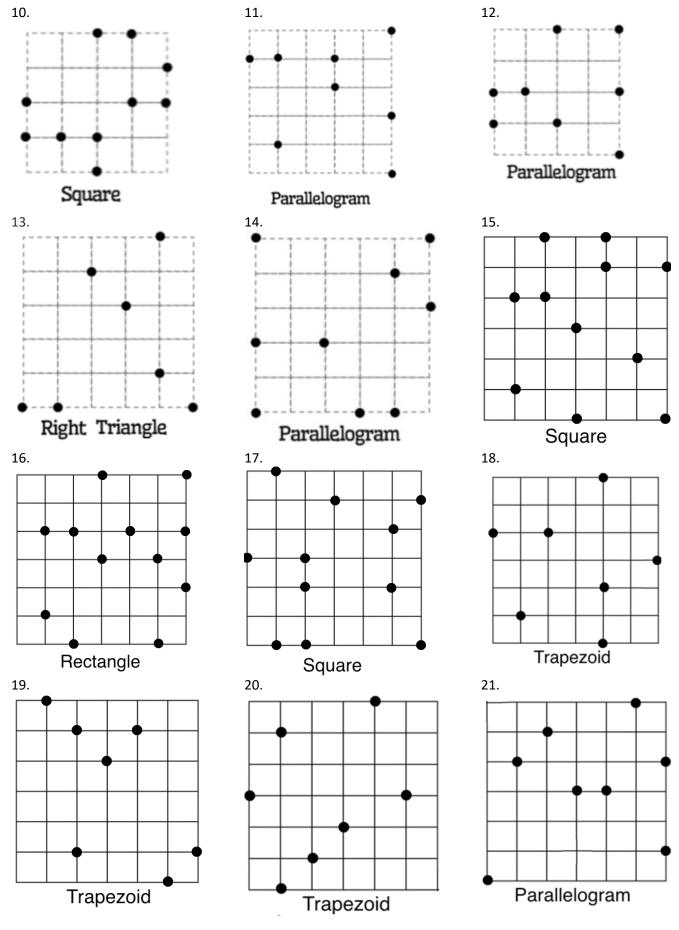


Zukei Puzzles

Name:

Zukei Puzzles are logic puzzles originally created by a Japanese person named Naoki Inaba, and I have added a few of my own. In each case, you need to connect 3 or 4 of the dots to create the indicated shape. Note – there will be some MPM1D-related follow-up!

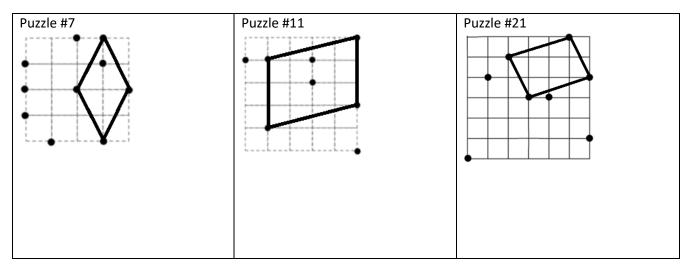




Zukei Puzzles - Follow up

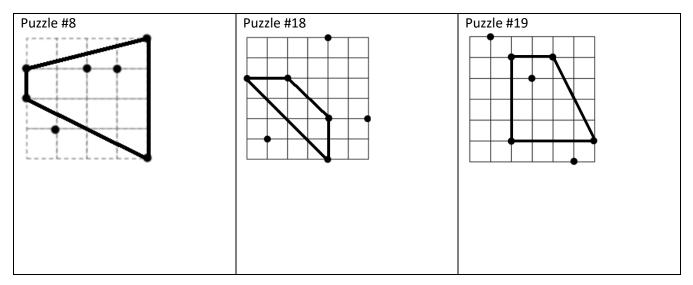
Recall: $Slope = \frac{\text{vertical distance}}{\text{horizontal distance}} = \frac{rise}{run}$

1. Consider Zukei puzzles #7, 11 and 21, which are all either parallelograms or rhombuses. Determine the slope of each side of each shape.



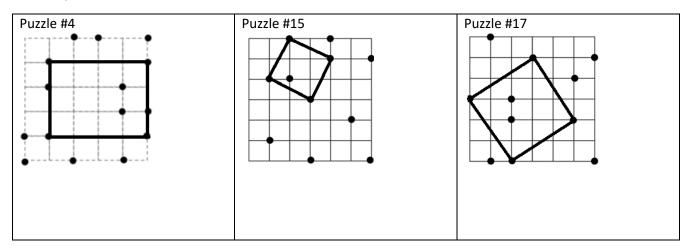
2. How many pairs of parallel sides does a parallelogram and rhombus have? How do your slopes from question #1 support this?

3. Consider Zukei puzzles #8, 18 and 19, which are all trapezoids. Determine the slope of each side of each shape. Remember to reduce each fraction.



4. How many pairs of parallel sides does a trapezoid have? How do your slopes from question #3 support this?

5. Consider Zukei puzzles #4, 15 and 17, which are all squares or rectangles. Determine the slope of each side of each shape. Remember to reduce each fraction.

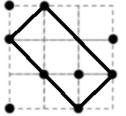


6. How many pairs of parallel sides do squares and rectangles have? How do your slopes from question #5 support this?

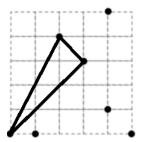
7. Squares and rectangles have sides that meet at 90°. We say the lines are _____

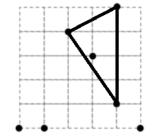
Examine the slopes you determined in question #5. Suggest how we might be able to tell whether lines are perpendicular from their slopes.

8. Determine the slopes for the rectangle in puzzle #3 below. Do these slopes make sense given your response in question #7? Why/why not?



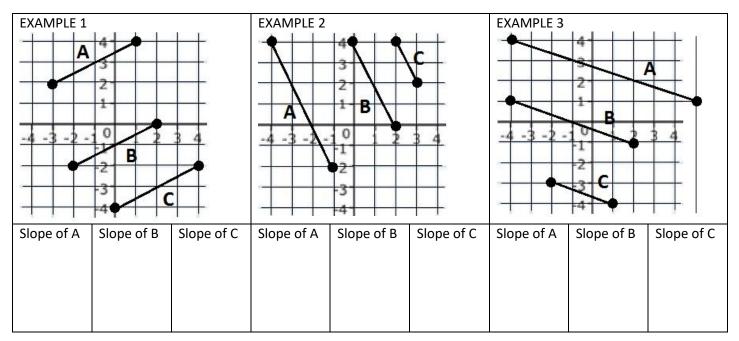
9. Two students say they've found a right angle triangle in #6. Use slopes to determine which is correct. Solution #1 Solution #2



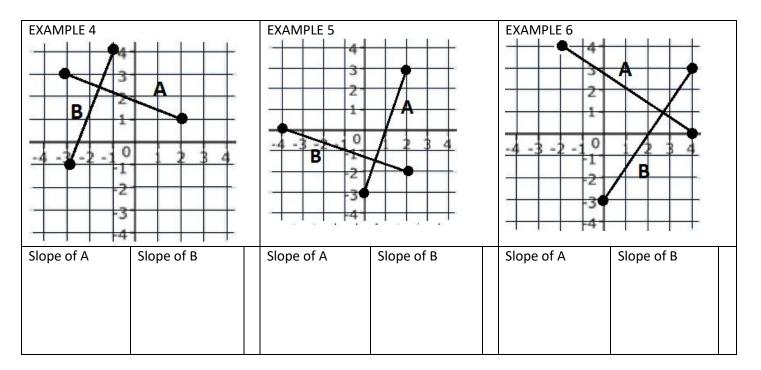


MPM 1D – Shapes and Slopes

Name: _____



How can we tell if lines are parallel?



How can we tell if two lines are perpendicular?

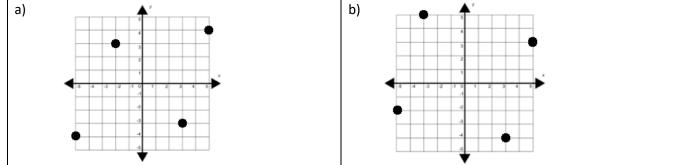
Working with Slopes – Parallel and Perpendicular

	1. Write whether these slopes are parallel, perpendicular, or neither							
a) —	$\frac{2}{3}$ and $-\frac{4}{6}$ _				e) 5 and	1 5 ———		
b) $\frac{-4}{3}$ and $\frac{3}{-4}$			f) $\frac{-1}{-5}$ and $\frac{1}{5}$					
c) $\frac{4}{5}$ and $\frac{5}{4}$				g) 2 and (undefined			
d) 3 and $-\frac{1}{3}$				h) $\frac{1}{2}$ and ().5			
2. H	ere are the slo	pes of som	e lines.					
$\frac{2}{3}$	ere are the slo $\frac{1}{3}$	3	$-\frac{3}{2}$	$\frac{4}{6}$	$\frac{6}{2}$	$-\frac{1}{3}$	$\frac{12}{4}$	2
a) Write all the s	lopes that are p	arallel		b) Wri	te all the slo	pes that are	perpendicul	lar

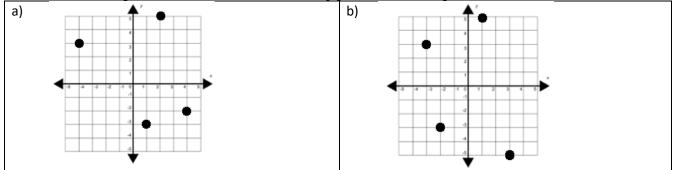
3. Give a slope that is perpendicular to each of the following slopes:

a) $m = \frac{2}{3}$	b) $m = -\frac{4}{5}$	c) m = 2	d) m = 0

4. Use slopes to determine if the following sets of points form a parallelogram.



5. Use slopes to determine if the following points form a trapezoid.



Making Shapes

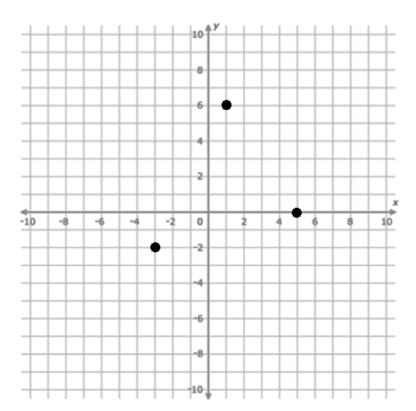
Name: _____

ON THIS PAGE, ONLY IDENTIFY POINTS FOR WHICH THE COORDINATES ARE INTEGERS, AND ONLY IDENTIFY POINTS THAT ARE ON THE GRID (THERE ARE MANY OTHERS OFF THE GRID)

1. a) What are the coordinates of the points?

b) Identify all possible locations for a 4th point that would result in a parallelogram

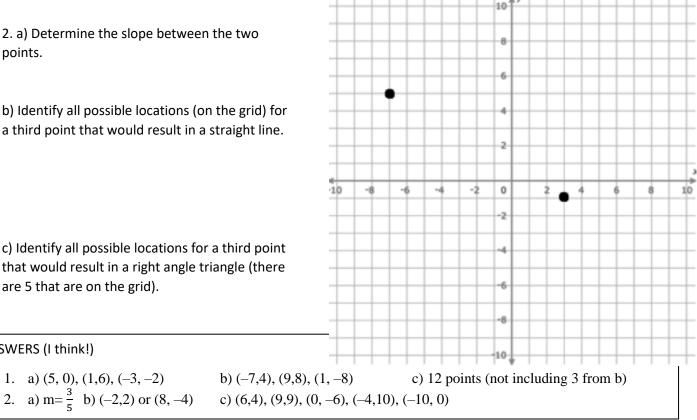
c) How many points will result in a trapezoid (not including the 3 points from part b)?



2. a) Determine the slope between the two points.

b) Identify all possible locations (on the grid) for a third point that would result in a straight line.

c) Identify all possible locations for a third point that would result in a right angle triangle (there are 5 that are on the grid).



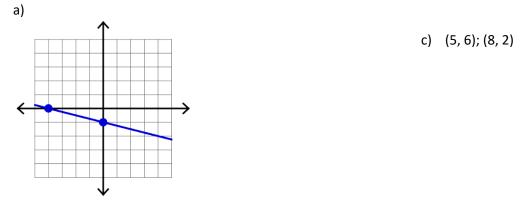
ANSWERS (I think!)

Calculating Slope from Points or Graphs

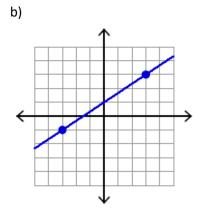
- The slope of a line is how steep it is
- We can find the slope of a line connecting two points (x_1, y_1) and (x_2, y_2) by this formula:

$$slope = m = \frac{rise}{run} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$$

Determine the slope.



d) (-1, 3); (5, 7)



e) (-5, 0); (-1; 2)

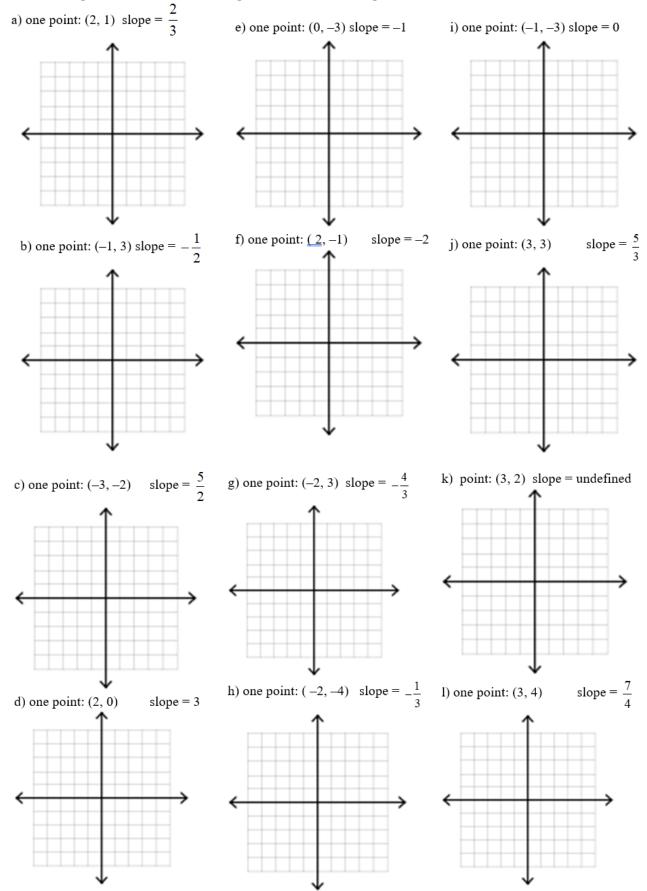
f) (4, -2); (-5, -11)

Calculate the slope between each pair of points. $slope = m = \frac{rise}{run} = \frac{y_2 - y_1}{x_2 - x_1} = \frac{\Delta y}{\Delta x}$ 1) (19, -16), (-7, -15) 2) (1, -19), (-2, -7) 3) (-4, 7), (-6, -4)

Examples: Given a point on a line and the slope of the line, find another point on the line.

a) Point: $(1, -2)$ Slope: $\frac{2}{3}$	Another Point:	b) Point:(-4, 3) Slope: -4	Another Point:	c) Point: (0, 0) Slope: $-\frac{4}{3}$	Another Point:
a) Point: (3, -4) Slope: 1	Another Point:	b) Point: (0, 4) Slope: $-\frac{3}{2}$	Another Point:	c) Point: (4, 2) Slope: 0	Another Point:

Given one point on a line and the slope, determine another point on the line.



<u>Slope – Mixed Problems...</u>

1. Calculate the slope between each pair of points. State whether the slope are parallel, perpendicular, or neither.

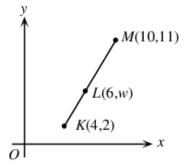
a) (4,5) and (2,1)	(6,2) and (10, 10)	
b) (5, 1) and (2, 2)	(6, 7) and (8, 2)	
c) (2,3) and (5,1)	(6,2) and (0,-2)	
d) (3, 2) and (8, 2)	(-4, 2) and (-4, 8)	

2. A line with a slope of $-\frac{15}{13}$ passes through the point (-15, 6). What is another point on the line? Explain.

3. Use slopes to determine if the following three points form a right angle.

a)	L(-4, 3)	b)	P(-1,-3)
	M(-2, -3)		Q(3,5)
	N(7, 0)		R(–5, 0)

- 4. Do the following three points form a straight line? Justify using slopes. A(13, 18) B(-5, 9) C(19, 21)
- 5. Point L lies on line segment KM as shown. What is the value of *w*? Show your work/thinking.



6. If the line that passes through the point (2, 7) and (*a*, 3*a*) has a slope of 2, what is the value of *a*? Show your work/thinking.

CARDBOARD PRISMS – CALCULATING COSTS

1. You need the following amounts of material. Determine the cost of the cardboard prism. Show your work. You only need to pay for what you use.

ITEM: Cardboard	ITEM: Noodles	ITEM: Glue	ITEM: Labour
YOU NEED: 900 cm ²	YOU NEED: 1400 mL	YOU NEED: 80 cm for edges	YOU NEED: 1.5 hours
		20 dabs (enough for 10 wall	
		braces)	
COST: 5000 cm ² costs \$10	COST: 2L costs \$5	COST: A glue stick costs	COST: Worker makes
		\$0.25 and can do 15 cm of	\$620 for her 40 hour
		edge or 4 dabs	week

2. You need the following amounts of material. Determine the cost of the cardboard prism. Show your work. You only need to pay for what you use.

ITEM: Cardboard	ITEM: Noodles	ITEM: Glue	ITEM: Labour
YOU NEED: 900 cm ²	YOU NEED: 1400 mL	YOU NEED: 80 cm for edges	YOU NEED: 1.5 hours
		20 dabs (enough for 10 wall	
		braces)	
COST: A 50 cm x 80 cm	COST: A box	COST: A pound of glue sticks	COST: Builder is paid 40%
piece normally costs \$16,	measuring	costs \$15. Each glue stick	more than Ontario's
but it is on sale for 25%	12 in x 12 in x 12 in	weighs 25 g. A glue stick can	minimum wage
off	costs \$7	do 20 cm of edge or 8 dabs	

Some common conversior	ns. You can look up others a	as needed, but state any c	onversion rates yo	ou use.
1 inch = 2.5 cm (approx.)	1 cm ³ = 1 mL	1 foot = 12 inches	1 kg = 1000 g	1 dozen = 12 items
1 m = 100 cm 1	m = 3.3 feet (approx.)	\$1 = 100 cents	1L = 1000 mL	1 pound = 454 g

	1.	2.
	Cardboard \$1.8	Cardboard \$2.7
ANSWERS	Noodles \$3.5	Noodles \$0.36
	Edge Glue \$1.33	Edge Glue \$3.3
	Dab Glue \$1.25	Dab Glue \$2.07
	Labour \$23.25	Labour \$29.40
	Total \$31.13	Total \$37.83

MPM1D CARDBOARD PRISMS – CALCULATING COST Name: _____

The cardboard prism you need to build requires the following materials:

Cardboard	Noodles	Edge Glue	Dab Glue	Labour
1200 cm ²	1450 mL	85 cm	6 wall braces (each brace has 2 dabs)	Will take an hour and a quarter

Calculate the cost to build the prism for each of the 4 countries below. In all cases, you only need to pay for the materials you use (eg. If you only need half a stick of glue, you don't need to pay for the entire stick).

TANZANIA							
1. Cardboard	2.	Noodles		3. Glue		4. Labour	
\rightarrow Cardboard		\rightarrow Noodles		\rightarrow For edges: it costs 2 cents per o	cm	\rightarrow The builder	
costs \$0.0025		cost \$0.75		of edge		is paid	
per square cm		per L		ightarrow For dabs: each dab costs 5 cen	ts	\$5/hour	
MONGOLIA							
1. Cardboard		2. Noodles		3. Glue	4	4. Labour	
→ Cardboard costs		\rightarrow 2 L of nood	es	ightarrow a glue stick costs \$1.25		\rightarrow The builder is	
\$1.50 for a piece	cost \$3.50			ightarrow each glue stick can do 50		paid \$275 for their	
measuring 500 square	re l			cm of edge, or 10 dabs		40 hour work	
cm						week	
NICARAGUA					1		
1. Cardboard		2. Noodles		3. Glue		4. Labour	
\rightarrow A piece of		ightarrow The first half		→A dozen glue sticks costs		\rightarrow The builder insists	
cardboard measuring		litre of noodles		\$5.50		on getting paid 20%	
50 cm x 80 cm costs		costs \$1.40.		ightarrow 2 glue sticks are needed	1	more than the Ontario	
\$6.25, but is on sale		\rightarrow After that,		to join 1 foot of edges		minimum wage	
for 20% off.		noodles cost		→ One glue stick can be			
		\$1.80 per litre		used for 25 dabs			
FIJI					1		
1. Cardboard		2. Noodles		3. Glue		4. Labour	
\rightarrow A cardboard sheet		\rightarrow Noodles cost		→ Glue costs \$6.60 per		ightarrow The builder	
measuring 2 feet by 3		\$5 per kg		pound		demands US\$500 for a	
feet costs \$25		\rightarrow One scoop of		ightarrow a 7 g stick of glue is		40 hour work week	
ightarrow Add 15% of the		noodles weighs		enough for 25 cm of edge,		ightarrow you still need to	
required cardboard		40 g and has a		or 12 dabs		pay in Canadian \$	
amount for wastage		volume of 74 r	mL				

Some common conversions. You can look up others as needed, but state any conversion rates you use.						
1 inch = 2.5 cm (appro	x.) 1 cm ³ = 1 mL	1 foot = 12 inches	1 kg = 1000 g	1 dozen = 12 items		
1 m = 100 cm	1 m = 3.3 feet (approx.)	\$1 = 100 cents	1L = 1000 mL	1 pound = 454 g		

ANSWERS						
Country	Cardboard	Noodles	Edge	Dab	Labour (\$)	Total (\$)
	(\$)	(\$)	Glue (\$)	Glue (\$)		
Tanzania	3	1.09	1.7	0.6	6.25	12.64
Mongolia	3.6	2.5375	2.125	1.5	8.59	18.35
Nicaragua	1.5	3.11	2.6	0.22	21	28.43
Fiji	6.39	3.92	0.35	0.1	20.31 (using exchange	31.07
					rate of 1.3)	